

# Exercise 17.1: Externality Pricing

## Recall

- externality pricing mechanism:
  - ① pick the outcome that maximizes the total welfare.
  - ② charge each buyer the difference between the optimal welfare without the buyer and the welfare of other buyers (from 1)

## Exercise 17.1: Externality Pricing

### Setup:

- two buyers 1 and 2, two houses A and B
- bids:

	House A	House B
Buyer 1	8	7
Buyer 2	6	3

### Questions:

- Which house does Buyer 2 get in the externality pricing mechanism?
- What is Buyer 2's payment?

# Lecture 17: Online Matching

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- matching markets
- maximum weight matching
- market clearing
- externality pricing mechanism  
(a.k.a, Vickrey-Clarke-Groves, VCG)

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## Today:

- maximum weight matching (cont)
- duality
- online matching
- greedy online matching

## Exercise 17.2: Matching Dual

### Recall

$$\begin{aligned} \text{Dual}(\mathbf{u}, \mathbf{p}) &= \min_{\mathbf{u}, \mathbf{p}} \sum_i u_i + \sum_j p_j \\ \text{s.t. } u_i + p_j &\geq v_{ij} \quad \forall i, j \end{aligned}$$

### Exercise 17.2: Matching Dual

#### Setup:

- two buyers 1 and 2, two houses A and B
- values:

	House A	House B
Buyer 1	8	7
Buyer 2	6	3

**Questions:** Identify the optimal dual utilities:  $u_1$ ?  $u_2$ ?